

# Online-Appendix zu

# " Demand Estimation for Solar Photovoltaics in the United States – An Instrumental Variable Approach"

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# **Appendix**

**Note**:

*Full sample* refers to the 'Tracking the Sun' data set as published by the LBNL (Barbose & Darghouth, 2019) without changes unless specified otherwise.

*Price sample* refers to the sample left after applying all price-related selection criteria described in section 3.4.1.2 'Data selection'.

*Estimation sample* refers to the sample left after applying all selection criteria, also non-price related, described in section 3.4.1.2 'Data selection'.

*Final sample* is the sample left for model estimation after dropping all observations which have missing values in one or more of the included variables described in section 3.5.1 'Preferred econometric model'.





Figure SEQ Figure \\* ARABIC 1. Median system size by customer category over time, 1998 to 2008 Note: Lines fitted using generalised additive model (GAM) smoother, displaying .95 confidence interval.



Figure SEQ Figure \\* ARABIC 2. Module efficiency by module technology and customer category, 2018 Source: LBNL Tracking the Sun data (full sample)



Figure SEQ Figure \\* ARABIC 3. Share of module technology over time Source: LBNL Tracking the Sun data (full sample)



Figure SEQ Figure \\* ARABIC 4. Median installed price per watt over time by customer category, 2008 to 2018 Note: Lines fitted using generalised additive model (GAM) smoother,

displaying .95 confidence interval.



A2. TTS Data: Exploratory Data Analysis

Figure SEQ Figure \\* ARABIC 5. PV installations by state and customer category in the full sample



Figure SEQ Figure \\* ARABIC 6. PV installations by sample and customer category, 1998 to 2008 Source: LBNL Tracking the Sun data (full sample)



Figure SEQ Figure \\* ARABIC 7. System size development over time Note: Only observations with system size (W) in [0, 20000] and installed after 2007 included. System size increases over time from about 4kW median size in 2008 to over 6kW in 2018. There are several outliers, particularly at the upper bound, most likely from non-residential systems. Source: LBNL Tracking the Sun data (full sample)



Figure SEQ Figure \\* ARABIC 8. System size by state over time, 2008 to 2018

Note: Only observations with system size (W) in [0, 20000] and installed after 2007 included. System size varies across states, especially in early years with fewer installations. Californian systems have a systematically lower median system size than most other states.



Figure SEQ Figure \\* ARABIC 9. Price per watt by state over time, 2008 to 2018 (w/o outliers) *Note:* Only observations with price per watt in [0, 10] included.<br>*Source:* LBNL Tracking the Sun data (full sample)



A3. Estimation Data: Selection

Figure SEQ Figure \\* ARABIC 10. Density plot of price per watt (w/o outliers)

Note: Only observations with price per watt in [0, 10] included. Density curve plotted with bandwidth .9 in blue. Median price shown by red solid line, .25 and .75 quantiles shown by red dotted lines, respectively. Source: LBNL Tracking the Sun data (full sample)



Figure SEQ Figure \\* ARABIC 11. Density plot of system size (w/o outliers)

Note: Only observations with system size (W) in [0, 20000] included. Density curve plotted in blue. Median size shown by red solid line, .25 and .75 quantiles shown by red dotted lines, respectively. Source: LBNL Tracking the Sun data (full sample)



Figure SEQ Figure \\* ARABIC 12. Polysilicon prices over time for four data sets, 2010 to 2019

Source: Bloomberg, for indices SSPSPSNC (China), SSPSPSNI (Non-China), SSPFPSNO (Global), SOLRAPS (Insight)



Figure SEQ Figure \\* ARABIC 13. Pearson correlation of polysilicon price data sets with PVinsights data Source: Bloomberg, for indices SSPSPSNC (China), SSPSPSNI (Non-China),

SSPFPSNO (Overall), SOLRAPS (Insight)



#### Figure SEQ Figure \\* ARABIC 14. Median polysilicon prices for four data sets

Source: Bloomberg, for indices SSPSPSNC (China), SSPSPSNI (Non-China), SSPFPSNO (Overall), SOLRAPS (Insight)



Figure SEQ Figure \\* ARABIC 15. Price per watt by tax rate  $Note:$  Regression line plotted in blue, fitted using generalised additive model (GAM) smoother and displaying .95 confidence interval. Source: LBNL Tracking the Sun data (estimation sample)



Figure SEQ Figure \\* ARABIC 16. Correlation matrix of continuous variables

Note: Pairwise Pearson correlation coefficients are calculated for relevant continuous variables. Some control variables as well as instrument data show high correlation, indicating that including all of them in the regression might result in collinearity problems.

Source: Own analysis, estimation sample



Figure SEQ Figure \\* ARABIC 17. Correlation matrix for continuous variables for California 2017 Note: Pairwise Pearson correlation coefficients are calculated for relevant continuous variables, holding state and year fixed. High correlation between some control variables and instruments becomes even more apparent, indicating that including all of them in the regression might result in collinearity problems. Some correlation coefficients are zero because there is no within-year variation. Source: Own analysis, estimation sample

## Data summary of estimation sample



Table SEQ Table \\* ARABIC 3. Data summary of the estimation sample

Note: Some variables related to incentive programs, e.g., rebate, PBI, and feed-in tariff payments show a large share of zero-values. As these most likely stem from incomplete data rather than true zeros, these variables will probably be of little use for the estimations. The control variables exhibit over 35% of missing values, which will cause a substantial reduction in observations used for the estimation. Source: Own analysis, estimation sample

A4. Estimation Data: Transformation



Figure SEQ Figure \\* ARABIC 18. Regression plots of system size (W) against selected variables Note: Regression lines fitted using generalised additive model (GAM) smoother, displaying .95 confidence interval.

Source: Own analysis, 50,000 observations randomly sampled without replacement from estimation sample



Figure SEQ Figure \\* ARABIC 19. Regression plots of system size (W) against selected variables after log-transformation

Note: Regression lines fitted using generalised additive model (GAM) smoother, displaying .95 confidence interval.

Source: Own analysis, 50,000 observations randomly sampled without replacement from estimation sample



Figure SEQ Figure \\* ARABIC 20. Regression plots of price per watt against selected variables Note: Regression lines fitted using generalised additive model (GAM) smoother, displaying .95 confidence interval.

Source: Own analysis, 50,000 observations randomly sampled without replacement from estimation sample



Figure SEQ Figure \\* ARABIC 21. Regression plots of price per watt against selected variables after log-transformation

Note: Regression lines fitted using generalised additive model (GAM) smoother, displaying .95 confidence interval.

Source: Own analysis, 50,000 observations randomly sampled without replacement from estimation sample



Figure SEQ Figure \\* ARABIC 22. Density plots of relevant variables  $Note: System Size (W)$ , Price per Watt, Tax Rate, Tax per Watt, and Rebate/Grant per Watt are right skewed. Module Efficiency is left skewed. Source: Own analysis, estimation sample



Figure SEQ Figure \\* ARABIC 23. Density plots of the log of relevant variables

Note: Taking the log relieves skewness in most of the variables. Source: Own analysis, estimation sample

# A5. Estimation Data: Summary



## Data summary of final sample

Table SEQ Table \\* ARABIC 4. Data summary of final sample Source: Own analysis, final sample

#### Summary statistics of final sample



Table SEQ Table \\* ARABIC 5. Summary statistics for numeric variables of the final sample Note: Original data, not log-transformed.

Source: Own analysis, final sample

#### Unique factor values of final sample



Table SEQ Table \\* ARABIC 6. Unique values for factor variables of the final sample

Source: Own analysis, final sample

#### Observations in final sample by Installation Year



#### **Observations in final sample by State**



# **Observations in final sample by New Construction**



## **Observations in final sample by Tracking**



# **Observations in final sample by Ground-Mounting**



## **Observations in final sample by Module Technology**



#### **Observations in final sample by MLPE**



Table SEQ Table \\* ARABIC 7. Distribution and share of installations by factor variables in the final sample

# A6. Regression Results



Table SEQ Table \\* ARABIC 8. First stage results for simple linear regression of selected instruments on Price per Watt

Note: Individual OLS regressions of potential instruments to evaluate their predictive power. Tax rate shows by far the highest coefficient of determination (.526), the combination with polysilicon price improves it very slightly.

Source: Own analysis, estimation sample



"p=0.05; ""p=0.01; """p=0.001

Table SEQ Table \\* ARABIC 9. IV regression results for simple linear regression of selected instruments on System Size

Note: Individual TSLS regressions using potential instruments. The best results in terms of R<sup>2</sup> and low residual standard error provide the regressions using tax rate as well as tax rate and polysilicon price as instruments.

Source: Own analysis, estimation sample



# Table SEQ Table \\* ARABIC 10. First stage regression results for the final model specification and different robustness checks

Note: First stage OLS regression results of instruments and explanatory variables on price per watt, using five different sets of instruments and four different sets of regressors. The combination of model (3) is selected for the final model as it shows the highest  $R^2$  (.992) and lowest standard errors while there is no 64 welfixellinessite in the evaluation or control mutables



#### Table SEQ Table \\* ARABIC 11. First stage results of robustness checks for the final model against alternative specifications

Note: First stage OLS regression results of instruments and explanatory variables on price per watt. The final model as baseline estimation compared to alternative specifications including a second-degree polynomial in the first stage, interaction of the fixed effects, quarterly time fixed effects, and no fixed effects. All use the same instruments polysilicon price and tax rate for price per watt.

Source: Own analysis, estimation sample



Figure SEQ Figure \\* ARABIC 24. Year fixed effects of final model

Note: Effects are provided relative to the baseline year 2010. They capture changes over time that are common for all states. Source: Own analysis, final sample



Figure SEQ Figure \\* ARABIC 25. State fixed effects of final model

Note: Effects are provided relative to the baseline state California. They capture differences across states that are constant over time.

Source: Own analysis, final sample



#### Figure SEQ Figure \\* ARABIC 26. Quarterly fixed effects of alternative specification

Note: Effects are provided relative to the baseline quarter Q1 in 2010. They capture changes over time that are common for all states.

Source: Own analysis, final sample

#### Median installed price per watt and tax rate by state



Table SEQ Table \\* ARABIC 12. Median price per watt and corresponding median tax rate by state Source: Own analysis, estimation sample

#### Variance inflation factor



Instruments: Polynilison Prise, Tax Rate<br>
Table SEQ Table V<sup>5</sup> ARABIC 13. Variance<br>
inflation factor for the final model<br>
Mote: VIF values below 5 indicate absence of<br>
severe multicollinearity problems, values<br>
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nsme="Book">6</br/>%ref-type><<ontributors>>>1</>xutho $\mathrm{rss}\sim\mathrm{subtov}\mathrm{Borel}$ -harmone (and the Gaustine Canadia Campainter (and the Campainter Campainter (and the Campainter Campainter (Present)<br>rever-duration (Present) (Ca



Table SEQ Table \\* ARABIC 14. IV regression results for four different income groups

Note: Observations are grouped by adjusted gross income per household (AGI/Household). Equal intervals in thousands of USD are (1) low: (16.5,442], (2) low/medium: (442,867], (3) medium/high: (867,1.29e+03], (4) high:  $(1.29e+03,1.72e+03)$ .<br>Source: Own analysis, estimation sample



Table SEQ Table \\* ARABIC 15. IV regression results for three different groups of population density Note: Observations are grouped by the number of households. Equal intervals in thousands are (1) low: (0.09,18.1], (2) medium: (18.1,36.2], (3) high: (36.2,54.3]. Source: Own analysis, estimation sample



Table SEQ Table  $\$ <sup>\*</sup> ARABIC 16. IV regression results by state *Note:* For Arizona and Texas, some explanatory factor variables did not provide any variation, such that they were excluded from the estimation for the respective subsamples.

Source: Own analysis, estimation sample

# A7. Model Evaluation





Instruments: Polysilicon Price, Tax Rate

Table SEQ Table \\* ARABIC 17. Diagnostic test results for final model

Note: Test on instrument relevance (Weak instruments), exogeneity of regressors (Wu-Hausman), and exogeneity of instruments (Sargan), including the test statistics and p-values. The instruments used are not weak and the regressors are endogenous while there is no evidence to assume endogeneity in the instruments. Source: Own analysis, final sample



Figure SEQ Figure \\* ARABIC 27. Test of OLS assumptions for the first stage of the final model Note: Plots to evaluate linearity assumption (observed vs. predicted values), i.i.d. assumption/ homoskedasticity (residuals vs. predicted values), and normality assumption (sample vs. theoretical quantiles) in the first stage.

Source: Own analysis, final sample



Figure SEQ Figure \\* ARABIC 28. Test of OLS assumptions for the second stage of the final model Note: Plots to evaluate linearity assumption (observed vs. predicted values), i.i.d. assumption/ homoskedasticity (residuals vs. predicted values), and normality assumption (sample vs. theoretical quantiles) in the second stage.

Source: Own analysis, final sample

# **Name Abbreviation Description Data source** System size (W) systemsizew The total rated direct-current (DC) output of the module arrays at standard test conditions. LNBL Price per watt priceperwatt The installed price per watt installed, prior to receipt of any incentives. LNBL Installation date installationdate The day the system was installed. For some data providers, the installation date may be based on the best available proxy, such as the date that an incentive claim was submitted or when the inspection was performed. LNBL Installation year installation year The year of installation, extracted from the installation date. LNBL Installation week installationweek The week of installation, extracted from the installation date. LNBL State stategroup The U.S. state the system is installed in. Rare states with less than 20,001 observations were grouped to 'other' states. LNBL Zip code zip zip The 5-digit zip code the system is installed in. LNBL Sales tax cost salestaxcost The calculated cost of sales taxes. This is estimated based on average sales tax rates for the given state and year, accounting for any sales tax exemptions that may exist for PV systems. Sales taxes, if applicable, are assumed to be levied only on hardware costs, which are assumed to represent 55% of the total installed price. LNBL Tax per watt taxperwatt that the sales tax cost per watt. Tax rate taxrate taxrate The sales tax rate applied on the installed price. LNBL Rebate or grant rebateorgrant rebateorgrant The pre-tax value of any up-front rebate or grant provided by the entity supplying the data. LNBL Rebate or grant per watt rebateorgrantperwatt The rebate or grant provided per watt. LNBL New construction newconstruction Indicates if the system was installed at the time of building construction. LNBL Tracking tracking tracking tracking Indicates if the system includes tracking equipment. LNBL

## **Variable overview from combined estimation data set**



**Table 18. Overview of variables used in or considered for the estimation**

*Note:* This is not an exhaustive overview of the variables contained in the data set and investigated in the study, but a selection of the most relevant ones. Some variables were calculated or derived from the original data sets.

# B1. Discussion of IV model assumptions

**(1)** In every linear regression, the number one assumption is that the conditional distribution of the error term given the exogenous regressors has a mean of zero  $(E(u_i|W_i) = 0)$ , i.e., error terms and the exogenous regressors are uncorrelated (Stock & Watson, 2020). This assumption is key as it makes the estimators unbiased. Omitted variables can cause the assumption to be violated. If there are further unobserved factors that influence the PV demand and that are simultaneously correlated with the regressors included in the model, then estimation results will be wrong in case these missing variables cannot be included in the model. As some data are not available or unobservable, this will be a relevant issue to be discussed in more detail.

**(2)** The second assumption for a valid IV estimation is that all variables are independent and identically distributed  $(i, i, d)$ , i.e., all observation samples  $(Y, X, \cdot)$  $W$ , Z) must be *i. i. d.* draws from their joint distribution (Stock & Watson, 2020). This assumption holds if the data are collected as random samples from a representative pool of observations. In many real-life applications this assumption is violated due to limited representativeness or time-series relationships. It shows that the way of collecting data is crucial. In this study, data used for estimation were reported mainly by incentive administrators in 30 states (Barbose & Darghouth, 2019). The representativeness is questionable as there might be a selection bias towards systems eligible for incentive payments, although this holds true for most. Furthermore, many observations stem from rather high-cost locations. That implies that the estimated effects might be valid for a reasonable subset of the installations rather than all installations in the U.S. This needs to be kept in mind for the interpretation and generalisability of the results.

**(3)** The third assumption is that there are no extreme outliers in the data, implying that the fourth moments measuring the kurtosis, i.e., the tail of the distribution, are finite. Luckily, the data at hand has been cleaned and pre-processed and obvious outliers have been removed<sup>27</sup>, wherefore one can assume this assumption to hold.

**(4)** The last and probably most important requirement is that all instruments are valid. This means that all instruments must be both *relevant* (not weak) and *exogenous* (not correlated to the error term), as already outlined in 3.2.2 above

<sup>&</sup>lt;sup>27</sup> See section 3.4.1.2 for details on data selection.

(Stock & Watson, 2020). If this is not the case, the resulting estimates might be biased much more than with an OLS estimation (Angrist & Krueger, 2001). Fortunately, there are ways to test relevance and exogeneity, at least for overidentified IV regressions. One solution to the problem of weak instruments is to estimate the reduced form equation, i.e., conducting an OLS regression of the dependent variable  $Y$  directly on the instruments  $Z$  and the exogenous variables  $W$ (Angrist & Pischke, 2008). The resulting estimates are unbiased and proportional to the coefficients of interest which can be inferred by rescaling (Angrist  $\&$ Krueger, 2001). Further, the relevance condition includes that there is no perfect multicollinearity between regressors. In practice, regressors are often partly correlated, e.g., module type and module efficiency might be related in this data set. However, the estimations are still valid as long as the collinearity is not perfect. Multicollinearity will be investigated by computing pairwise correlations as well as the variance inflation factor<sup>28</sup> (VIF) (James et al., 2013).

<sup>&</sup>lt;sup>28</sup> "The VIF is the ratio of the variance of *i* when fitting the full model divided by the variance of j if fit on its own." The smallest possible value indicating absence of multicollinearity is 1, a VIF value exceeding 5 or 10 shows a collinearity problem (p. 101, James et al. (2013)).

# B2. Data Processing

Firstly, I convert all data types into the correct format for estimation and change system size from kilowatts to watts. To improve the estimation quality, I also generate more predictors from the given data. Most importantly, I create per-watt-values for installed price, rebate or grant and sale tax. Furthermore, I calculate the tax rate applied by dividing the total sales tax paid by 55% of the installed price as it is assumed that sales taxes are levied only on the hardware costs of the installation. I also remove the four-digit zip code extension given for some observations to obtain five-digit zip codes for every installation. Additionally, I add the installation year, month, and week as variables to the data set, while making sure that one year only has 52 distinct weeks.

Additionally, I group systems by the state they are installed in, selecting all states with more than 20,000 installations and grouping the rest into 'other' states (7.8% of the estimation sample). Likewise, I cluster observations by customer segment into residential, small non-residential, and large non-residential and I group module technology into polysilicon, monocrystalline silicon, and other technologies to obtain a significant number of observations per category. For some installations, up to three different modules are listed in the original data set. However, for the second and third module, less than 4% and 1% of all observations, respectively, show data on module technology. Therefore, the second and third module values on technology, efficiency, etc. are only considered if information for the preceding first or second is not available. Thereby, I merge the information on module technology, efficiency, and use of microinverter for all modules belonging to one installation.

Subsequently, I add dummies to indicate a premium module with efficiency no less than 20% (about 8% of the full sample and in line with Barbose and Darghouth (2019)), the presence of MLPE, and an indicator for whether the observation meets the criteria to be included in the price sample or not. Finally, I factor all non-numeric variables, mapping them to integer values to be able to use them for subsequent estimations.

It needs to be kept in mind that several observations exhibit missing data for one or more of the relevant variables. I do not impute missing data or outliers which is more common in machine learning, as there is substantial uncertainty about most of the missing values. However, simply discarding observations with missing predictor values can likewise lead to biased estimates, especially if

installations with missing values differ systematically from the completely observed cases or if there are only very few complete observations in the sample, significantly reducing the data finally used for estimation (Gelman & Hill, 2006). This could be relevant in this estimation as missing data are often related to the phase down of incentive programs which have primarily been used for data collection (Barbose & Darghouth, 2019).

The above represents a brief summary of the most relevant data processing steps. For more details, please refer to the corresponding code provided in the R Markdown file.

# B3. Data Transformation

After left joining all additional data sources to the estimation sample constructed from the TTS data set, the whole sample needs to be transformed in order to enable the estimation of elasticities. First, I convert tax rate and module efficiency values to percentages. Subsequently, to specify a log-log model, I log-transform all continuous variables. For those which exhibit zero values, I add one to the data in order to still map zero values to zero after taking the log, as log(1) equals 0 (Benoit, 2011).

Standardisation and normalisation of variables is reasonable in case the model requires comparable scales. However, this is not the case for linear algorithms, wherefore I refrain from any such transformations in order to maintain high interpretability of the estimation results. The resulting pooled cross-sectional data set is well-suited for studying dynamics of change and transition behaviour like the adaption of a new technology (Baltagi, 2008; Dielman, 1983). Unfortunately, as for some states and years, there are substantially more data points available, the panel is notably unbalanced.